

USEFUL RELATIONSHIPS BETWEEN  $k_{\text{eff}}$ ,  $B_m^2$  and  $B_g^2$

The reactivity of a fissile system can be described by

$$k_{\text{eff}} = \frac{k_{\infty}}{1 + M^2 B_g^2} \quad \text{where} \quad \begin{aligned} k_{\text{eff}} &= \text{effective multiplication constant} \\ k_{\infty} &= \text{multiplication constant for an infinite amount of the fissile material} \\ B^2 &= \text{geometrical buckling of the system} \\ M^2 &= \text{migration area of the neutrons (about 25 to 30 cm for H/fissile atom } > 20) \end{aligned}$$

at critical  $k_{\text{eff}} = 1.0$  and  $B_m^2 = B_g^2$ , where

$B_m^2$  = material buckling of the fissile material, or

$$1 = \frac{k_{\infty}}{1 + M^2 B_m^2}$$

Substituting, we have:

$$k_{\text{eff}} = \frac{1 + M^2 B_m^2}{1 + M^2 B_g^2}$$

and we can determine the reactivity of a given system with a known geometry and material, or

$$B_m^2 = \frac{k_{\text{eff}}(1 + M^2 B_g^2) - 1}{M^2}$$

where the geometry and the limiting  $k_{\text{eff}}$  is known and the material buckling is desired, or

$$B_g^2 = \frac{1}{M^2} \left[ \frac{1 + M^2 B_m^2}{k_{\text{eff}}} - 1 \right]$$

where the limiting  $k_{\text{eff}}$  and the material is known and the limiting geometry is desired.

These equations may be used for rough determinations of the desired parameters for simple geometrical shapes with no interaction.